

**Statistisk tolkning av data – Jämförelse av två
medelvärden erhållna vid parvisa observationer**

**Statistical interpretation of data – Comparison of
two means in the case of paired observations**

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Statistisk tolkning av data – Styrka av hypotestest avseende medelvärde och varians

Denna standard utgörs av den engelska versionen av den internationella standarden ISO 3494–1976, Statistical interpretation of test results – Power of tests relating to means and variances.

Standarden dokumenterar en viktig statistisk teknik. Den kan utgöra en referens om överenskommelse träffas att använda de i standarden ingående metoderna. Som exempel må nämnas i anvisningar för provning eller statistisk kontroll av processer och produkter. Den kan användas i utbildning, men utgör ingen lärobok. I standarden anges ej i vilka konkreta sammanhang den är tillämplig.

Den i denna standard angivna internationella standarden ISO 2854 gäller som svensk standard SS 01 42 11 – ISO 2854, Statistisk tolkning av data – Skattning och hypotestest avseende medelvärde och varians.

Se även SS 01 42 01, Statistik - Terminologi.

Statistical interpretation of data – Power of tests relating to means and variances

This standard consists of the English version of the international standard ISO 3494–1976, Statistical interpretation of test results – Power of tests relating to means and variances.

The standard documents an important statistical technique. It can be used as a reference in case of agreements where one considers that the methods in the standard ought to be used, for instance in instructions for testing or statistical inspection of processes and products. It can be used in education, but is no textbook. No specific situation where the standard can be applied is stated in it.

The international standard, ISO 2854, mentioned in this standard is valid as Swedish standard SS 01 42 11 – ISO 2854, Statistical interpretation of data – Techniques of estimation and tests relating to means and variances.

See also SS 01 42 01, Statistics – Terminology.

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Prefixet SS införs som beteckning för svensk standard utgiven 1978-01-01 och senare. Vid revidering av äldre standarder ersätter SS prefixen SEN, SIS och SMS. Den numeriska delen behålls i regel oförändrad. Standard utarbetad av SEK får 7-siffrig numerisk del med siffran 4 före de klassificerande sex siffrorna.

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Statistical interpretation of data – Power of tests relating to means and variances

SECTION ONE : COMPARISON TESTS

GENERAL REMARKS

1) This International Standard follows on from ISO 2854, *Statistical interpretation of data – Techniques of estimation and tests relating to means and variances*.

The conditions of application of this International Standard are as stated in the "General remarks" in ISO 2854. It will be recalled that the tests used are valid if the distribution of the observed variable is assumed to be normal in each population (see comments on paragraph 3 of the "General remarks" in ISO 2854). ISO 2854 is concerned only with the type I risk (or significance level). This International Standard puts forward notions of the type II risk and of power of the test.

2) It will also be recalled that the type I risk is the probability of rejecting the null hypothesis (tested hypothesis) if this hypothesis is true (case of two-sided tests), or the maximum value of this probability (case of one-sided tests). The non-rejection of the null hypothesis produces, in practice, acceptance of the hypothesis, yet non-rejection does not mean that the hypothesis is true.

Accordingly, the type II risk, designated by β , is the probability of not rejecting the null hypothesis when it is false. The complement of the probability of committing the error of the second kind ($1 - \beta$) is the "power" of the test (see "Historical note" following these general remarks).

3) Whereas the value of the type I risk is chosen by the consumers according to the consequences that could arise from that risk (either of the values $\alpha = 0,05$ or $\alpha = 0,01$ is commonly employed), the type II risk is dependent on the true hypothesis (the null hypothesis H_0 being false), i.e. the alternative hypothesis to the null hypothesis. In the comparison of a population mean with a given value m_0 , for example, a specific alternative corresponds to a value of the population mean of $m \neq m_0$ being a deviation $m - m_0 \neq 0$. As a general rule, in tests of comparison of means and variances, the alternatives are defined by the values that might be assumed by a parameter.

4) The operating characteristic curve of a test is the curve which shows the value β of the type II risk as a function of the parameter defining the alternative. β is also dependent on the value chosen for the type I risk, on size(s) of sample(s) and on the nature of the test (two-sided or one-sided).

In the tests of comparison of means, β also depends on the standard deviation of the population(s). Where this is unknown, the risk β cannot be known exactly.

5) The operating characteristic curves allow the following problems to be solved.

a) **problem 1** : For a given alternative and given size of sample, determine the probability β of not rejecting the null hypothesis (type II risk).

b) **problem 2** : For a given alternative and a given value of β determine the size of sample to be selected.

Although a single series of curve sets allows both problems to be solved, two series of sets will be presented, in order to facilitate practical applications :

– **sets 1.1 to 14.1**, giving the risk β as a function of the alternative, for $\alpha = 0,05$ or $\alpha = 0,01$ and for different values of the size(s) of sample.

– **sets 1.2 to 14.2**, giving the size(s) of sample to be selected as a function of the alternative, for $\alpha = 0,05$ or $\alpha = 0,01$ and for different values of the risk β .

6) Attention is drawn to the practical significance of interpreting statistics by means of tests of hypotheses and curves. When testing a hypothesis such as $m = m_0$ (or $m_1 = m_2$), it is generally desired to know whether it can be concluded with little risk of mistake, that m does not differ too greatly from m_0 (or m_1 does not differ too greatly from m_2). Moreover, the choice of the value $\alpha = 0,05$ or $\alpha = 0,01$ for the type I risk associated with the test has a degree of arbitrariness. Therefore, it may be useful to examine what the result of the test would be with values close to m_0 (or value of the difference $D = m_1 - m_2$ close to 0), possibly using both values of the type I risk $\alpha = 0,05$ and $\alpha = 0,01$ and, in these circumstances, to evaluate by means of the operating characteristic curves the risk β associated with different alternatives.

7) The sets of curves which are given in section two of this International Standard are described and discussed in six clauses which correspond to the tables in ISO 2854.

The detailed correspondence between the different sets, the problems which they allow to be solved, the clauses of this International Standard and the tables of ISO 2854, appear at the top of the group of sets.

HISTORICAL NOTE

The concepts "type I risk" and "type II risk" were introduced by J. Neyman and E. S. Pearson in an article which appeared in 1928. Subsequently, these authors considered that the complement of the probability of committing the error of the second kind – which they called "power" of the test, in its aptitude to reveal as significant a specified alternative to the null hypothesis (tested hypothesis) – was in general an easier concept for the users to understand. It is this "power", or the probability of revealing a given deviation from the null hypothesis, which they designated by the symbol β .

It is moreover not necessary to introduce the term "power". One can more simply speak of the probability that a statistical test applied to a sample, at a significance level α , reveals that a parameter λ of the population differs

(when such is truly the case) by at least a given quantity from the specified value λ_0 , or, in relation to it, in a ratio at least equal to a given number.

The change in notation was probably introduced in the United States by users of industrial applications of statistics, in order that the "consumer's risk", when designated by β , might be taken into consideration at the same time as the "producer's risk α ".

The symbol β was adopted for the type II risk in ISO 3534, *Statistics – Vocabulary and symbols*, and it has therefore been adopted with the same significance in this International Standard. However, as this symbol is used, and will continue no doubt to be used, with both meanings in statistical literature, it is advisable to find out, in each case of use, the meaning which is effectively attributed to it.

1 COMPARISON OF A MEAN WITH A GIVEN VALUE (VARIANCE KNOWN)

See table A of ISO 2854.

1.1 Notations

n = sample size

m = population mean

m_0 = given value

σ = standard deviation for the population

1.2 Tested hypotheses

For a two-sided test, the null hypothesis is $m = m_0$, the alternative hypothesis corresponding to $m \neq m_0$.

For a one-sided test, the null hypothesis is

- a) either $m \leq m_0$, the alternative hypothesis corresponding to $m > m_0$;
- b) or $m \geq m_0$, the alternative hypothesis corresponding to $m < m_0$.

1.3 Problem 1 : n being given, determine the risk β

For the different values of m , the alternative is defined by the parameter λ ($0 < \lambda < \infty$), with

- a) $\lambda = \frac{\sqrt{n} |m - m_0|}{\sigma}$ (two-sided test) alternatives $m \neq m_0$
- b) $\lambda = \frac{\sqrt{n} (m - m_0)}{\sigma}$ (one-sided test $m \leq m_0$) alternatives $m > m_0$
- c) $\lambda = \frac{-\sqrt{n} (m - m_0)}{\sigma}$ (one-sided test $m \geq m_0$) alternatives $m < m_0$

According to the case, the set to be consulted is

- 1.1 (two-sided test) type I risk $\alpha = 0,05$
- 2.1 (two-sided test) type I risk $\alpha = 0,01$
- 3.1 (one-sided test) type I risk $\alpha = 0,05$
- 4.1 (one-sided test) type I risk $\alpha = 0,01$

β is the ordinate of the point of the abscissa λ on the curve $\nu = \infty$ of the suitable test.

1.4 Problem 2 : β being given, determine the size n

For the different values of m , the alternative is defined by the parameter λ ($0 < \lambda < \infty$), with

- a) $\lambda = \frac{|m - m_0|}{\sigma}$ (two-sided test) alternatives $m \neq m_0$

b) $\lambda = \frac{m - m_0}{\sigma}$ (one-sided test $m \leq m_0$) alternatives $m > m_0$

c) $\lambda = -\frac{m - m_0}{\sigma}$ (one-sided test $m \geq m_0$) alternatives $m < m_0$

According to the case, the set to be consulted is

- 1.2 (two-sided test) type I risk $\alpha = 0,05$
- 2.2 (two-sided test) type I risk $\alpha = 0,01$
- 3.2 (one-sided test) type I risk $\alpha = 0,05$
- 4.2 (one-sided test) type I risk $\alpha = 0,01$

n is the ordinate of the point on the abscissa λ on the straight line (broken line) which corresponds to the given value β .

1.5 Example

A producer of cotton yarn guarantees, for each of the batches he delivers, a mean breaking load (expressed in newtons) at least equal to $m_0 = 2,30$. The consumer only agrees to accept the batches after having verified on elements of yarn of a given length, taken from different bobbins, that the one-sided test, as described in ISO 2854, does not lead to a rejection of the hypothesis $m \geq m_0 = 2,30$, the value chosen for the type I risk being $\alpha = 0,05$ (α is therefore here the “producer’s risk”).

The consumer knows from experience that the mean of the different batches may vary, but the dispersion of the breaking loads within any one batch is practically constant with a standard deviation $\sigma = 0,33$.

1.5.1 The consumer envisages selecting $n = 10$ bobbins per batch, and wishes to know the probability that he will not reject the hypothesis $m \geq 2,30$ (hence to accept the batch) where in fact the mean breaking load would be $m = 2,10$.

The set to be consulted is set 3.1. The value of the parameter λ for $m = 2,10$ is

$$\lambda = \frac{-\sqrt{n} (m - m_0)}{\sigma} = \frac{\sqrt{10} (2,30 - 2,10)}{0,33} = 1,92$$

The straight line $\nu = \infty$ gives for 100β the value $36 : \beta = 0,36$ or 36% .

1.5.2 This value being considered by the consumer as much too high, he decides to select a sample of sufficient size for the risk β to be reduced to $0,10$ (or 10%) if $m = 2,10$.

The set to be consulted is set 3.2. The value of the parameter λ for $m = 2,10$ is

$$\lambda = -\frac{m - m_0}{\sigma} = \frac{2,30 - 2,10}{0,33} = 0,61$$

The value of n , read on the straight lines (broken) $\beta = 0,10$ is $n = 22$.

**2 COMPARISON OF A MEAN WITH A GIVEN VALUE
(VARIANCE UNKNOWN)**

See table A' of ISO 2854.

IMPORTANT NOTE

The type II risk β depends on the true value σ of the standard deviation for the population, which is unknown. Hence, β can only be known approximately, and this provided that an order of magnitude of σ is available. In the absence of any valid previous information, one will take for σ the estimation s obtained from the sample.

It is strongly recommended that the influence on the values read from the operating characteristic curve of an error made for the standard deviation σ should be considered. The inaccuracy can be very great where σ has been estimated from a sample of small size : allowance for this situation can be made by placing s within the confidence limits for σ calculated by the method in table F of ISO 2854.

2.1 Notations

n = sample size

m = population mean

m_0 = given value

σ = standard deviation for the population (which will be replaced by an approximate value)

ν = $n - 1$

2.2 Tested hypotheses

For a two-sided test, the null hypothesis is $m = m_0$, the alternative hypotheses corresponding to $m \neq m_0$.

For a one-sided test, the null hypothesis is

a) either $m \leq m_0$, the alternative hypotheses corresponding to $m > m_0$;

b) or $m \geq m_0$, the alternative hypotheses corresponding to $m < m_0$.

2.3 Problem 1 : n being given, determine the risk β

For the different values of m , the alternative is defined by the parameter λ ($0 < \lambda < \infty$), with

a) $\lambda = \frac{\sqrt{n} |m - m_0|}{\sigma}$ (two-sided test) alternatives $m \neq m_0$

b) $\lambda = \frac{\sqrt{n} (m - m_0)}{\sigma}$ (one-sided test $m \leq m_0$) alternatives $m > m_0$

c) $\lambda = -\frac{\sqrt{n} (m - m_0)}{\sigma}$ (one-sided test $m \geq m_0$) alternatives $m < m_0$

1) That is, the probability that when using the Student test with the significance level $\alpha = 0,05$, the value $m = 2,10$ is not revealed to be significantly lower than $m_0 = 2,30$.

According to the case, the set to be consulted is

- 1.1 (two-sided test) type I risk $\alpha = 0,05$
- 2.1 (two-sided test) type I risk $\alpha = 0,01$
- 3.1 (one-sided test) type I risk $\alpha = 0,05$
- 4.1 (one-sided test) type I risk $\alpha = 0,01$

β is the ordinate of the point on the abscissa λ on the curve $\nu = n - 1$ of the suitable set.

2.4 Problem 2 : β being given, determine the size n

For the different values of m , the alternative is defined by the parameter λ ($0 < \lambda < \infty$), with

a) $\lambda = \frac{|m - m_0|}{\sigma}$ (two-sided test) alternatives $m \neq m_0$

b) $\lambda = \frac{m - m_0}{\sigma}$ (one-sided test $m \leq m_0$) alternatives $m > m_0$

c) $\lambda = -\frac{m - m_0}{\sigma}$ (one-sided test $m \geq m_0$) alternatives $m < m_0$

According to the case, the set to be consulted is

- 1.2 (two-sided test) type I risk $\alpha = 0,05$
- 2.2 (two-sided test) type I risk $\alpha = 0,01$
- 3.2 (one-sided test) type I risk $\alpha = 0,05$
- 4.2 (one-sided test) type I risk $\alpha = 0,01$

n is the ordinate of the point of the abscissa λ on the curve which corresponds to the given value β .

2.5 Example

The example is the same as in 1.5, but the consumer does not know the exact value of the standard deviation of the breaking loads. He knows, however, from experience, that this is almost certainly within the limits

$$\sigma_1 = 0,30 \quad \sigma_5 = 0,45$$

2.5.1 The consumer envisages selecting $n = 10$ bobbins per batch, and wishes to know the probability that he will not reject the hypothesis $m \geq 2,30$ (hence to accept the batch), while in fact the mean breaking load would be $m = 2,10$.¹⁾

The set to be consulted is set 3.1. The values of the parameter λ which correspond to the extreme values of σ are

$$\lambda_1 = \frac{\sqrt{10} (2,30 - 2,10)}{0,30} = 2,1$$

$$\lambda_5 = \frac{\sqrt{10} (2,30 - 2,10)}{0,45} = 1,4$$

The corresponding values of 100β read (by interpolation) $\nu = 9$ are 40 and 64; i.e.

$$\beta_I = 0,40 \text{ (or 40 \%)}$$

$$\beta_S = 0,64 \text{ (or 64 \%)}$$

2.5.2 The consumer wishes, in the most unfavourable hypothesis ($\sigma = \sigma_S = 0,45$), β not to exceed 0,10 (or 10 %) if $m = 2,10$.

The set to be consulted is set 3.2, curve $\beta = 0,10$, with

$$\lambda = \frac{2,30 - 2,10}{0,45} = 0,44$$

For $\beta = 0,10$ and $\lambda = 0,44$, one finds n in the order of 45.

If, after inspection of several batches, it is found that the standard deviation is stable, σ can be estimated with greater precision : the sample size to be taken from the following batches can probably be reduced, with the guarantees of the producer and the consumer being maintained.

3 COMPARISON OF TWO MEANS (VARIANCES KNOWN)

See table C of ISO 2854.

3.1 Notations

	Population No. 1	Population No. 2
Sample size	n_1	n_2
Mean	m_1	m_2
Variance	σ_1^2	σ_2^2
Standard deviation of the difference of the mean of the two samples	$\sigma_d = \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$	

3.2 Tested hypotheses

For a two-sided test, the null hypothesis is $m_1 = m_2$, the alternative hypotheses corresponding to $m_1 \neq m_2$.

For a one-sided test, the null hypothesis is

- a) either $m_1 \leq m_2$, the alternative hypotheses corresponding to $m_1 > m_2$;
- b) or $m_1 \geq m_2$, the alternative hypotheses corresponding to $m_1 < m_2$.

3.3 Problem 1 : n_1 and n_2 being given, determine the risk β

For the different values of the difference $m_1 - m_2$, the alternative is defined by the parameter λ ($0 < \lambda < \infty$), with

- a) $\lambda = \frac{|m_1 - m_2|}{\sigma_d}$ (two-sided test) alternatives $m_1 \neq m_2$
- b) $\lambda = \frac{m_1 - m_2}{\sigma_d}$ (one-sided test $m_1 \leq m_2$) alternatives $m_1 > m_2$
- c) $\lambda = \frac{m_2 - m_1}{\sigma_d}$ (one-sided test $m_1 \geq m_2$) alternatives $m_1 < m_2$

According to the case, the set to be consulted is

- 1.1 (two-sided test) type I risk $\alpha = 0,05$
- 2.1 (two-sided test) type I risk $\alpha = 0,01$
- 3.1 (one-sided test) type I risk $\alpha = 0,05$
- 4.1 (one-sided test) type I risk $\alpha = 0,01$

β is the ordinate of the point on the abscissa λ on the curve $\nu = \infty$ of the suitable set.

When the total size of the two samples is fixed, $n_1 + n_2 = 2n$, the best efficiency (β minimum) is obtained with :

$$\frac{n_1}{\sigma_1} = \frac{n_2}{\sigma_2}$$

hence

$$n_1 = 2n \frac{\sigma_1}{\sigma_1 + \sigma_2}$$

$$n_2 = 2n \frac{\sigma_2}{\sigma_1 + \sigma_2}$$

$$\lambda = \sqrt{2n} \frac{|m_1 - m_2|}{\sigma_1 + \sigma_2}$$

$$\left(\lambda = \sqrt{\frac{n}{2}} \frac{|m_1 - m_2|}{\sigma}, \text{ if } \sigma_1 = \sigma_2 = \sigma \right)$$

3.4 Problem 2 : β being given, determine the sizes n_1 and n_2

Using, according to the case, set 1.1, 2.1, 3.1 or 4.1, the curve $\nu = \infty$ allows the problem to be solved in the general case. The ordinate β corresponds to the point on the abscissa λ of this curve, and any pair (n_1, n_2) is suitable on the condition that

$$\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2} = \left(\frac{m_1 - m_2}{\lambda} \right)^2$$

The most economical sample ($n_1 + n_2$ minimum) is such that

$$\frac{n_1}{\sigma_1} = \frac{n_2}{\sigma_2}$$

hence

$$n_1 = \sigma_1 (\sigma_1 + \sigma_2) \left(\frac{\lambda}{m_1 - m_2} \right)^2$$

$$n_2 = \sigma_2 (\sigma_1 + \sigma_2) \left(\frac{\lambda}{m_1 - m_2} \right)^2$$

$$\left(n_1 = n_2 = 2 \left(\frac{\lambda \sigma}{m_1 - m_2} \right)^2, \text{ if } \sigma_1 = \sigma_2 = \sigma \right)$$

In the particular case where $\sigma_1 = \sigma_2 = \sigma$, $n_1 = n_2 = n$, it is more suitable to define, for the different values of the difference $m_1 - m_2$, the alternative by the parameter λ ($0 < \lambda < \infty$), with

$$a) \lambda = \frac{|m_1 - m_2|}{\sigma \sqrt{2}} \text{ (two-sided test) alternatives } m_1 \neq m_2$$

$$b) \lambda = \frac{m_1 - m_2}{\sigma \sqrt{2}} \text{ (one-sided test } m_1 \leq m_2) \text{ alternatives } m_1 > m_2$$

$$c) \lambda = \frac{m_2 - m_1}{\sigma \sqrt{2}} \text{ (one-sided test } m_1 \geq m_2) \text{ alternatives } m_1 < m_2$$

and to use according to the case, one of the following sets :

- 1.2 (two-sided test) type I risk $\alpha = 0,05$
- 2.2 (two-sided test) type I risk $\alpha = 0,01$
- 3.2 (one-sided test) type I risk $\alpha = 0,05$
- 4.2 (one-sided test) type I risk $\alpha = 0,01$

n is the ordinate of the point on the abscissa λ on the straight line (broken line) which corresponds to the given value β .

3.5 Example

A producer of cotton yarn has modified his process, but according to his declaration, the mean breaking load remains the same ($m_1 = m_2$), m_1 corresponding to the old process and m_2 to the new.

The consumer is prepared to adopt the new process, but wishes to verify the declaration of the producer, by carrying out on elements of yarn of a given length taken from different bobbins, the two-sided test of the hypothesis $m_1 = m_2$ as described in ISO 2854, with for the value of the type I risk $\alpha = 0,05$ (α is therefore here the "producer's risk").

The consumer knows, from experience, that for all the productions of this producer, the dispersion of the breaking load is practically constant and characterized by a standard deviation $\sigma = 0,33$.

3.5.1 The consumer envisages selecting 10 bobbins from a batch of each of the two processes, and wishes to know the probability that he will not reject the hypothesis $m_1 = m_2$ (hence to accept the batch of the new process) while in fact $|m_1 - m_2|$ would be equal to 0,30.

The set to be consulted is set 1.1, with

$$\lambda = \frac{|m_1 - m_2|}{\sigma_d}$$

$$|m_1 - m_2| = 0,30$$

$$\sigma_d = \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} = \sqrt{\frac{2}{n}} \sigma = \sqrt{\frac{2}{10}} \times 0,33 = 0,1476$$

$$\lambda = \frac{0,30}{0,1476} = 2,03$$

The curve $\nu = \infty$ gives for 100 β the value 47 : $\beta = 0,47$ or 47 %.

3.5.2 This value being considered by the consumer as much too high, he decides to select samples of a sufficiently large size for the risk β to be reduced to 0,10 (or 10 %) when $m_1 - m_2 = 0,30$.

The set to be consulted is set 1.2, with

$$\lambda = \frac{|m_1 - m_2|}{\sigma \sqrt{2}} = \frac{0,30}{0,33 \sqrt{2}} = 0,64$$

The value of n , read on the straight line (broken line) $\beta = 0,10$, is $n = 26$.